

# Development of Empirical Formulae for Estimating Ship Performance

by

Masaru TSUJIMOTO\*, Mariko KURODA\*, Naoto SOGIHARA\*  
and Akiko SAKURADA\*

## Abstract

A ship performance simulator called Vessel Performance Evaluation Tool in Actual Seas (VESTA) has been developed, which requires the input of detailed ship data or results of tank tests. Except for the ship designer or ship builder, it is difficult to input such data. To support input into VESTA assuming it is used at shipping companies, a program called United Tool for Assessment of a Ship has been developed. However for information service providers, it is necessary to additionally estimate data such as the displacement, longitudinal centre of buoyancy, draught and trim of a ship in operation, parameters relating to the estimation of wind forces, propeller characteristics and rudder forces, and specific fuel consumption for initial estimation. Therefore, empirical formulae using recent ship data and geometric relationships have been developed.

These empirical formulae are not only useful for information service providers but also for the initial estimating ship performance.

---

\* Fluids Engineering & Hull Design Department

Received 平成30年10月26日

Accepted 平成31年1月22日

## Contents

1. Introduction	92
2. Development of empirical formulae	92
2.1 Block coefficients	92
2.2 Water plane area coefficient	94
2.3 Longitudinal centre of buoyancy	94
2.4 Draught and trim at ballast load condition	96
2.5 Draught and trim correction for area exposed to wind	97
2.6 Length overall	99
2.7 Propeller diameter	100
2.8 Expanded blade area ratio of a propeller	100
2.9 Rudder area	102
2.10 Specific fuel consumption	104
3. Comprehensive evaluation	105
4. Conclusions	105
Acknowledgements	105
References	106

## 1. Introduction

When a ship navigates on the sea, speed decreases and fuel consumption increases due to winds and waves. A ship performance simulator called Vessel Performance Evaluation Tool in Actual Seas (VESTA) has been developed to simulate ship operation in such a situation<sup>1), 2)</sup>. However, VESTA requires the input of detailed ship design data. As shipping companies wishing to simulate ship performance during operation cannot obtain the detailed data without cooperation of the shipyard, it is necessary to estimate the ship design data. To solve this problem, a program called United Tool for Assessment of a Ship (UNITAS) to estimate the hull form and ship performance has been developed<sup>3), 4)</sup>. UNITAS uses some of the empirical formulae of a program called Hull Optimization Program for Economy (HOPE) Light<sup>5)</sup>.

For information service providers, such as a weather routing service, it is necessary to additionally estimate displacement, longitudinal centre of buoyancy, draught and trim of a ship during operation, parameters relating to the estimation of wind forces, propeller characteristics and rudder forces, and specific fuel consumption. Therefore, empirical formulae using recent ship data and geometric relationships have been developed.

## 2. Development of empirical formulae

## 2.1 Block coefficients

Since ship performance changes depending on the displacement, it is necessary to estimate when the displacement value during a voyage is unknown.

The block coefficient at the design load condition ( $C_{Bdes}$ ) is expressed using Eq. (1).

$$C_{Bdes} = \frac{\nabla_{des}}{L_{pp} B_{max} d_{mid}} \quad (1)$$

where  $\nabla_{des}$  is the displacement volume at the design load condition,  $L_{pp}$  is the ship length between perpendiculars,  $B_{max}$  is the maximum ship breadth, and  $d_{mid}$  is the midship draught at the design load condition.

When  $C_{Bdes}$  is unknown, it is estimated using the regression formula (Eq. (2)), which was translated to match recent ships based on the Heckscher formula<sup>6)</sup> (Eq. (3)).

$$C_{Bdes} = \begin{cases} \text{Min}(C_{BH} + 0.08, 0.875) & \text{for Bulker, Tanker and General cargo ship} \\ \text{Min}(C_{BH}, 0.875) & \text{for Container ship} \\ \text{Min}(C_{BH} - 0.08, 0.875) & \text{for RoRo ship} \end{cases} \quad (2)$$

$$C_{BH} = 1.04 - 1.67Fr \quad (3)$$

$$Fr = \frac{V}{\sqrt{L_{pp}g}} \quad (4)$$

where  $Fr$  is the Froude number,  $V$  is the design speed, and  $g$  is the gravitational acceleration. Fig. 1 shows the relation between  $C_{Bdes}$  and  $Fr$  using data that can be opened for public.

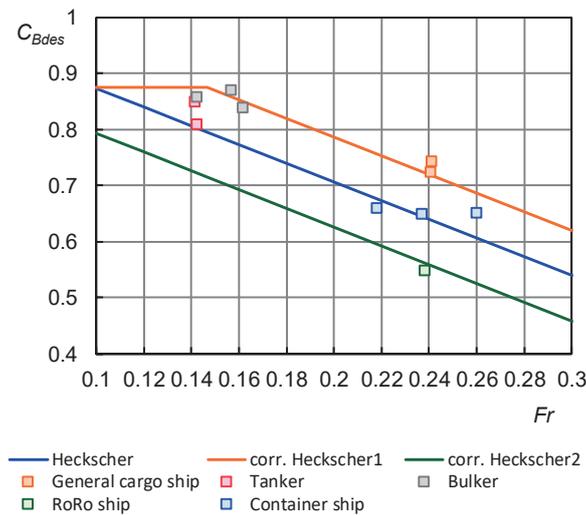


Fig. 1 Estimation of block coefficient at design load condition.

Assuming that the waterline shape is constant, i.e., the waterline area ( $A_w$ ) is constant, against draught change, actual displacement is expressed using Eq. (5), where  $d_v$  is the midship draught during a voyage. From Eq. (5), the block coefficient during a voyage ( $C_{Bv}$ ) can be expressed using Eq. (6). Here,  $C_w$  is the water plane area coefficient and its estimation will be discussed in Section 2.2.

$$\nabla_v = \nabla_{des} - A_w(d_{mid} - d_v) \quad (5)$$

$$C_{Bv} = C_{Bdes} \frac{d_{mid}}{d_v} - C_w \left( \frac{d_{mid}}{d_v} - 1 \right) \quad (6)$$

$$C_w = \frac{A_w}{L_{pp}B_{max}} \quad (7)$$

## 2.2 Water plane area coefficient

Estimation of  $C_w$  is necessary for estimating  $C_{Bv}$  and is described below.

Based on the data of a chart of the Shipbuilding Design Handbook<sup>6)</sup>,  $C_w$  can be estimated using the regression formulas on the prismatic coefficient ( $C_P$ ). The chart plotting recent ship data is shown in Fig. 2. The empirical formula is derived as Eq. (8). If  $C_P$  is unknown, it can be estimated using the regression formula for the midship section coefficient ( $C_M$ ) (Eq. (10))<sup>5)</sup>. The relations between  $C_P - C_B$  and  $C_M - C_B$  are also shown in Fig. 2.

$$C_w = \begin{cases} 0.845C_P + 0.211 & \text{for Bulker, Tanker and General cargo ship} \\ 0.845C_P + 0.287 & \text{for Container ship and RoRo ship} \end{cases} \quad (8)$$

$$C_P = \frac{C_B}{C_M} \quad (9)$$

$$C_M = \begin{cases} -6.6698C_B^4 + 22.631C_B^3 - 28.838C_B^2 + 16.368C_B - 2.4978 & \text{for } 32.2\text{m} \leq B_{max} \leq 32.26\text{m} \text{ and } 0.4 \leq C_B \leq 0.9 \\ -7.0219C_B^4 + 23.589C_B^3 - 29.771C_B^2 + 16.755C_B - 2.5556 & \text{for } B < 32.2\text{m}, 32.26\text{m} < B_{max} \text{ and } 0.4 \leq C_B \leq 0.9 \end{cases} \quad (10)$$

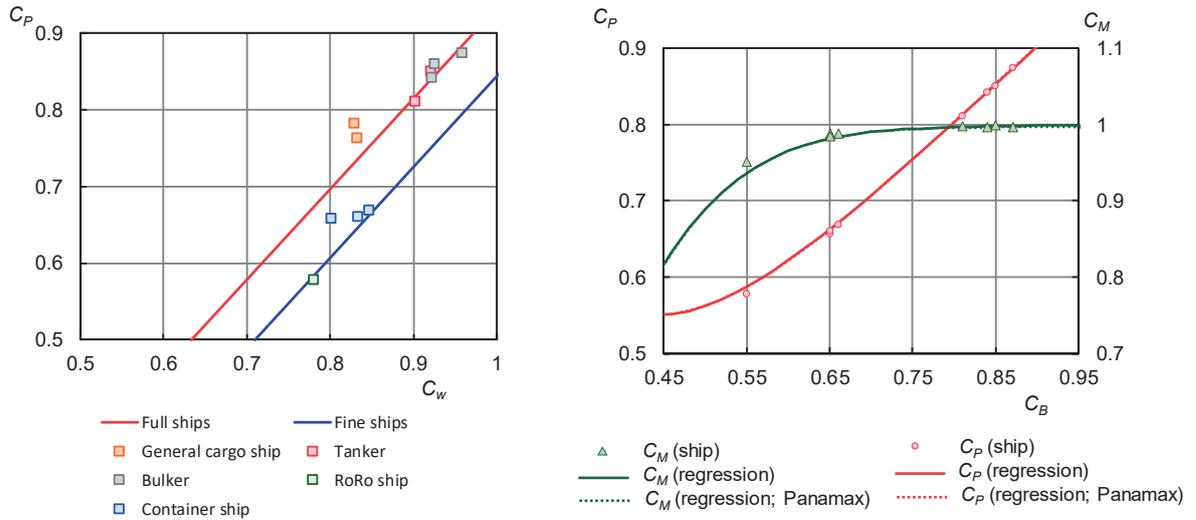


Fig. 2 Empirical relations (left;  $C_P - C_w$ , and right;  $C_P - C_B$  and  $C_M - C_B$ ).

## 2.3 Longitudinal centre of buoyancy

The longitudinal centre of buoyancy is important for performance estimation. If this value is obtained at the voyage load condition, it is better to use that value. However, if it is not obtained, an estimation formula is needed.

The distance from the midship to the longitudinal centre of buoyancy ( $X_{CB}$ ) is converted to  $l_{CB}$  ( $\%L_{pp}$ , which is the ratio of  $L_{pp}$ ). The relation is shown in Eq. (11). A positive  $X_{CB}$  is defined as from the midship to the bow, which is shown in Fig. 3, whereas a positive  $l_{CB}$  is defined here as from the midship to the stern.

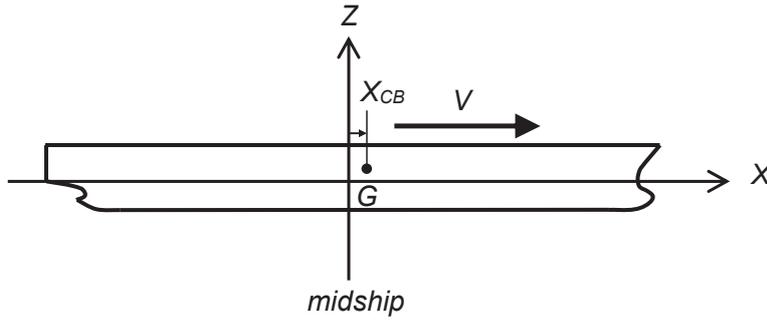


Fig. 3 Coordinate system.

$$X_{CB} = -l_{CB} \frac{L_{pp}}{100} \tag{11}$$

1) Estimating the longitudinal centre of buoyancy at the design load condition ( $l_{CB}$ ).

The  $l_{CB}$  at the design load condition is estimated using Eq. (12)<sup>5)</sup>.

$$l_{CB} = -23.0161911C_{Bdes} + 15.0527428 + 44.5 dFr \tag{12}$$

$$dFr = Fr - Fr_{STD} \tag{13}$$

$$Fr_{STD} = -0.4233695C_{Bdes} + 0.4933884 \tag{14}$$

2) Estimating the longitudinal centre of buoyancy at the voyage load condition ( $l_{CBv}$ )

The  $l_{CB}$  at the voyage load condition ( $l_{CBv}$ ) is estimated using Eq. (15), which matches the value from Eq. (11) at the design load condition.

$$l_{CBv} = -23.0161911C_{Bdes} + 15.0527428 + 44.5 dFr_v \tag{15}$$

$$dFr_v = Fr - Fr_{STDv} \tag{16}$$

$$Fr_{STDv} = -0.4233695C_{Bv} + 0.4933884 \tag{17}$$

3) Validation

To validate Eq. (15),  $X_{CB}$  for various voyage conditions is compared with the ship data. For this, Eq. (18) is used instead of Eq. (12) for a different draught.

$$l_{CBv} = -23.0161911C_{Bv} + 15.0527428 + 44.5 dFr_v \tag{18}$$

The validation is carried out for a bulk carrier and a roll-on/roll-off (RoRo) vehicle carrier. The principal dimensions of each ship are shown in Table 1, and the results are shown in Fig. 4, where  $dN$  is the ratio of the design to voyage draughts.

From Fig. 4,  $X_{CB}$  from Eq. (18) shows the opposite tendency to that derived from ship data, but  $X_{CB}$  from Eq. (15) shows the right tendency.

Table 1 Principal dimensions.

Dimensions	Bulk carrier	RoRo vehicle carrier
Ship length between perpendiculars ( $L_{pp}$ )	217.487 m	190.0 m
Maximum ship breadth ( $B_{max}$ )	32.26 m	32.26 m
Midship draught ( $d_{mid}$ )	14.0 m	9.0 m
Block coefficient at the design load condition ( $C_{Bdes}$ )	0.851	0.55
Design speed ( $V$ )	14.5 knots	20.0 knots

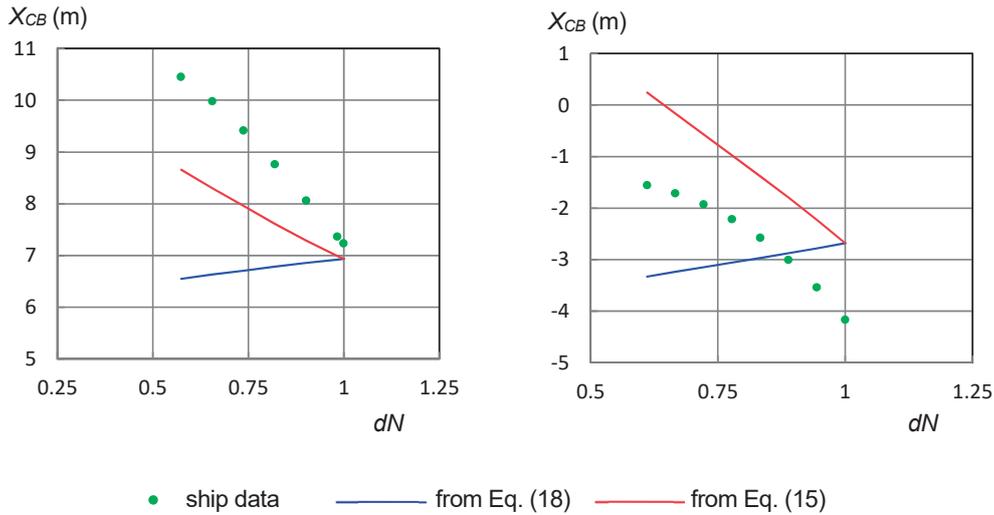


Fig. 4 Validation of  $X_{CB}$  (left; Bulk carrier, right; RoRo vehicle carrier).

### 2.4 Draught and trim at ballast load condition

When simulating the ship performance at the ballast load condition, information on the draught and the trim is required as well as  $C_B$  and  $X_{cb}$  value. However, if it is not obtained, it must be estimated. If the draught and trim are known in addition to the principal dimensions, it is possible to estimate the hull form at the ballast load condition by using UNITAS<sup>3),4)</sup>.

Using tankers, bulk carriers, and general cargo ships of the recent ship data, the midship draught at the ballast load condition ( $d_{mb}$ ) and the trim ( $trim$ ) are varied, as shown in Fig. 5, where  $d_m$  is the midship draught at the design load condition, and  $D_P$  is the propeller diameter. Eqs. (19) and (20) show the banded empirical relations.

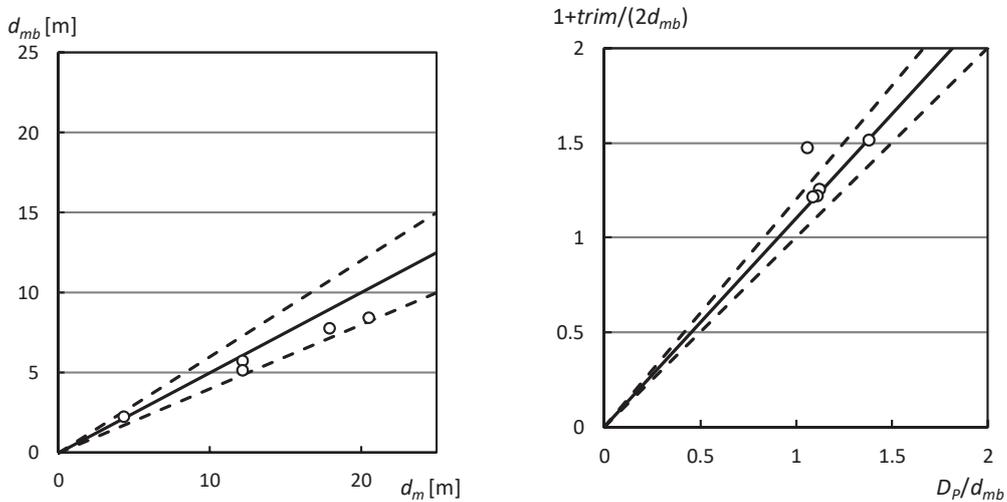


Fig. 5 Empirical relations for draught and trim at ballast load condition.

$$d_{mb} = \begin{cases} 0.4d_m & \text{lower line} \\ 0.5d_m & \text{average line} \\ 0.6d_m & \text{higher line} \end{cases} \quad (19)$$

$$1 + \frac{trim}{2d_{mb}} = \begin{cases} D_P / d_{mb} & \text{small trim} \\ 1.1D_P / d_{mb} & \text{average trim} \\ 1.2D_P / d_{mb} & \text{large trim} \end{cases} \quad (20)$$

From Eq. (20), *trim* is expressed as Eq. (21).

$$trim = \begin{cases} 2(D_p - d_{mb}) & \text{small trim} \\ 2(1.1D_p - d_{mb}) & \text{average trim} \\ 2(1.2D_p - d_{mb}) & \text{large trim} \end{cases} \quad (21)$$

When estimating the draught and trim at the ballast condition, the average lines in Eqs. (19) and (21) can be used, however, in order not to expose the propeller,  $trim \geq 0$  is required for Eq. (21).

## 2.5 Draught and trim correction for area exposed to wind

Regression formulae have been developed to estimate wind forces<sup>7)</sup>, and empirical formulae have also been developed for the input parameters of these formulae<sup>8)</sup> and are implemented in VESTA<sup>4)</sup> and UNITAS<sup>3), 4)</sup>. However, considering the ship condition during operation, it is necessary to estimate or correct the values at ballast load condition.

These input parameters are illustrated in Fig. 6, where  $A_T$  is the transverse projected area above the waterline including superstructures,  $A_L$  is the lateral projected area above the waterline including superstructures,  $A_{OD}$  is the lateral projected area of superstructures above the upper deck,  $C_{dis}$  is horizontal distance from midship section to centre of  $A_L$ ,  $H_{BR}$  is the height of top of superstructure (e.g., bridge), and  $H_C$  is the height from the waterline to centre of  $A_L$ . The subscript 0 means the value at even keel. The correction of the parameters for draught and trim change is carried out using the geometrical relations.

The draught variation ( $\Delta d$ ) is expressed using Eqs. (22) and (23), where the subscript *a* means aft, *f* means fore, and 0 means the draught at even keel.

$$\Delta d_a = d_a - d_{a0} \quad (22)$$

$$\Delta d_f = d_f - d_{f0} \quad (23)$$

Fig. 6 shows various ship conditions. The red line shows the waterline at even keel.

From the geometric relations,  $A_T$  is expressed using Eq. (24).

$$A_T = A_{T0} + \max(-\Delta d_a, -\Delta d_f) \cdot B_{max} \quad (24)$$

The increased  $A_L$  from even keel is approximated as a trapezoidal shape,  $A_L$  is approximated using Eq. (25). It is not necessary to estimate  $A_{OD}$  since it does not change along with the draught and trim change.

$$A_L = A_{L0} + \frac{1}{2} L_{pp} (-\Delta d_a - \Delta d_f) \quad (25)$$

From the geometric relations,  $H_{BR}$  is expressed using Eq. (26).

$$H_{BR} = H_{BR0} + \max(-\Delta d_a, -\Delta d_f) \quad (26)$$

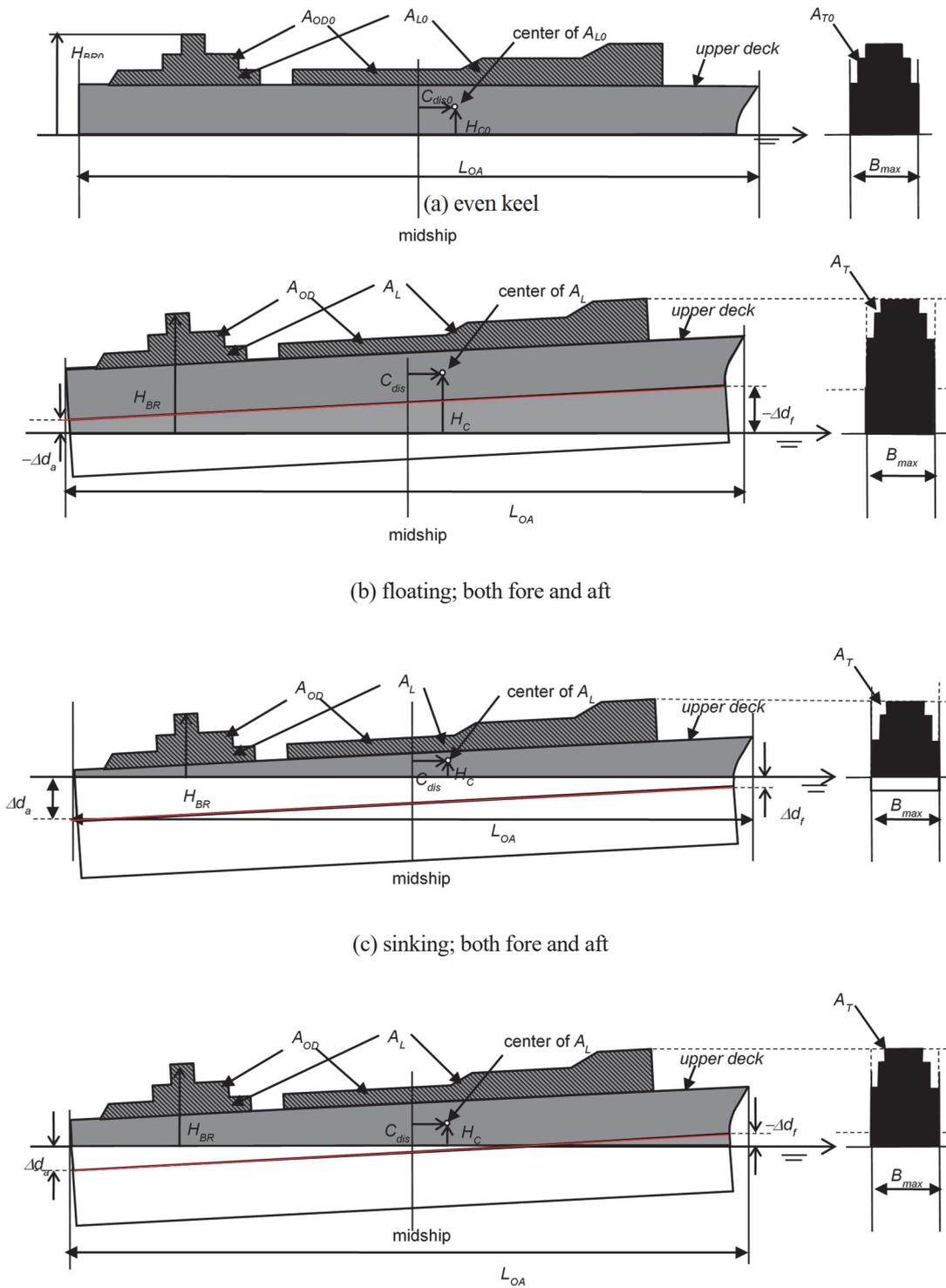


Fig. 6 Ship conditions.

The increased  $A_L$  from even keel ( $A_{inc}$ ) is approximated as a trapezoid, the area  $A_{inc}$  is estimated using Eq. (27).

$$A_{inc} = \frac{1}{2} L_{pp} (-\Delta d_a - \Delta d_f) \tag{27}$$

The horizontal distance ( $C_{inc}$ ) from the midship to the centre of the increased trapezoid is expressed using Eq. (28), and the height ( $H_{Cinc}$ ) from the waterline for the increased trapezoid is expressed using Eq. (29).

$$C_{inc} = \begin{cases} \frac{\Delta d_f - \Delta d_a}{6(\Delta d_a + \Delta d_f)} L_{pp} & (\Delta d_a + \Delta d_f \neq 0) \\ 0 & (\Delta d_a + \Delta d_f = 0) \end{cases} \quad (28)$$

$$H_{Cinc} = \begin{cases} \frac{\Delta d_f^2 + \Delta d_a \Delta d_f + \Delta d_a^2}{-3(\Delta d_a + \Delta d_f)} & (\Delta d_a + \Delta d_f \neq 0) \\ 0 & (\Delta d_a + \Delta d_f = 0) \end{cases} \quad (29)$$

From the area ratio,  $C_{dis}$  and  $H_C$  can be expressed using Eqs. (30) and (31), respectively.

$$C_{dis} = \frac{A_{L0} C_{dis0} + A_{inc} C_{inc}}{A_{L0} + A_{inc}} \quad (30)$$

$$H_C = \frac{A_{L0} \left\{ H_{C0} + \frac{-\Delta d_f + \Delta d_a}{L_{pp}} \left( \frac{L_{pp}}{2} + C_{dis0} \right) \right\} + A_{inc} H_{Cinc}}{A_{L0} + A_{inc}} \quad (31)$$

### 2.6 Length overall

Since the length overall ( $L_{OA}$ ) is related to the estimated wind forces, it is necessary to determine if this value is known or not known. If  $L_{OA}$  is known, it might be restricted due to a regulation or law and can be used. Otherwise, a regression formula derived from ship data is needed. Fig. 7 shows the relation between  $L_{OA}$  and  $L_{pp}$  from recent ship data. Equation (32) is the regression formula. For a RoRo vehicle carrier of  $190 \text{ m} \leq L_{pp} \leq 192 \text{ m}$ , it is better to use  $L_{OA}=200 \text{ m}$ .

$$L_{OA} = 1.04L_{pp} \quad (32)$$

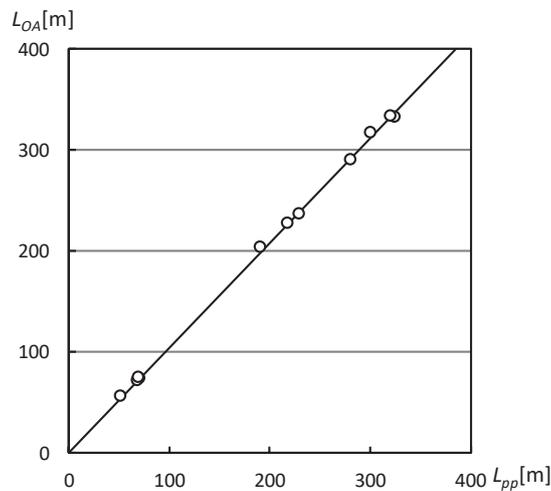


Fig. 7 Relation between  $L_{OA}$  and  $L_{pp}$ .

## 2.7 Propeller diameter

To make an estimation of required power of a ship, it is necessary to input the  $D_P$  and propeller characteristics in open water. These characteristics can be estimated using UNITAS<sup>3), 4)</sup>. If  $D_P$  is not known, it is necessary to estimate it.

The  $D_P$  can be estimated using Eq. (33)<sup>5)</sup>.

$$D_P = (C_1 d_a + C_2) d_a \quad (33)$$

where  $d_a$  is the draught at aft,  $C_1$  and  $C_2$  are the coefficients for propeller diameter, the values of which are shown in Table 2. The relation between  $D_P$  and  $d_a$  is shown in Fig. 8.

Table 2 Coefficients for propeller diameter.

Ship type	$C_1$	$C_2$
Container ship	0.0	0.650
RoRo ship	-0.0020	0.710
Bulker	-0.0080	0.600
Tanker	-0.0044	0.575

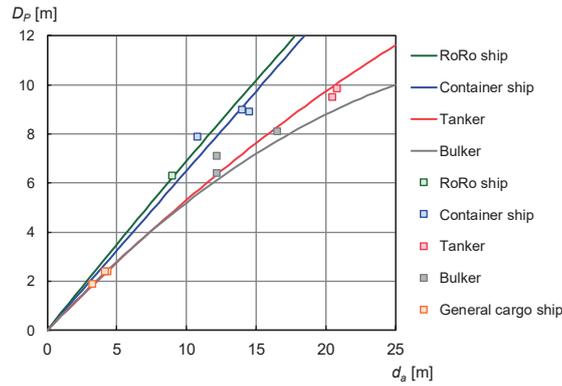


Fig. 8 Relation between  $D_P$  and  $d_a$ .

## 2.8 Expanded blade area ratio of a propeller

When estimating propeller characteristics in open water, chart-based estimation can be done, and it is implemented in UNITAS<sup>3), 4)</sup>. To use the chart, it is necessary to input the expanded blade area ratio ( $a_E$ ).

An estimation method for  $a_E$  was proposed by Ito<sup>9)</sup>. The method derives the relation between  $K=PS/(V_s D_P^2 a_E)$  and  $N_p D_P$ , where  $PS$  is the power of the main engines at  $NOR$  in PS,  $V_s$  is the ship speed at  $NOR$  of 0% sea margin in knots, and  $N_p$  is the rate of the propeller revolution in rpm. For three-blade propellers,  $a_E$  should be increased by 5% to apply it. Based on the method, similar charts are published<sup>10), 11)</sup>. The combined chart is shown in Fig. 9, in which the unit of the parameters are changed, i.e.,  $PS'$  is the power of the main engines at  $NOR$  in kW,  $V_s'$  is the ship speed at  $NOR$  of 0% sea margin in m/s, and  $n_p'$  is the rate of the propeller revolution at  $NOR$  in rps.

Since the evaluation conditions are difficult for practical use, the definition of ship speed and power is changed. The parameters are redefined as  $K_p = MCR / (V_{des} D_P^2 a_E)$  and  $n_p D_P$ , as shown in Fig. 10, where  $MCR$  is the maximum continuous rate of the main engines in kW,  $V_{des}$  is the designed speed in m/s, and  $n_p$  is the rate of the propeller revolution at  $MCR$  in rps.

Although comparison between Fig. 9 and Fig. 10 is difficult because of changing parameters, the recent ship data are divided into the two groups; full ships (tankers, bulkers, and general cargo ships) and fine ships (RoRo and container ships). Therefore, the empirical formula is expressed as Eq. (34). The parameters are listed in Table 3.

The evaluation data are 4 to 6 blade propellers and  $a_E$  ranging from 0.4 to 0.65 for full ships and from 0.65 to 0.8 for fine ships.

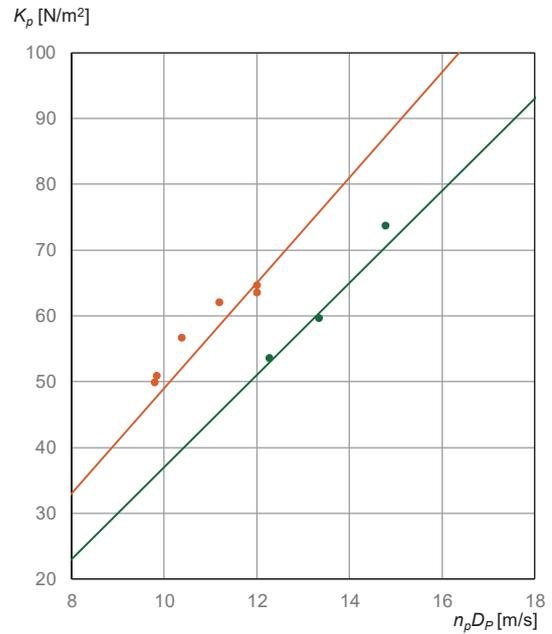
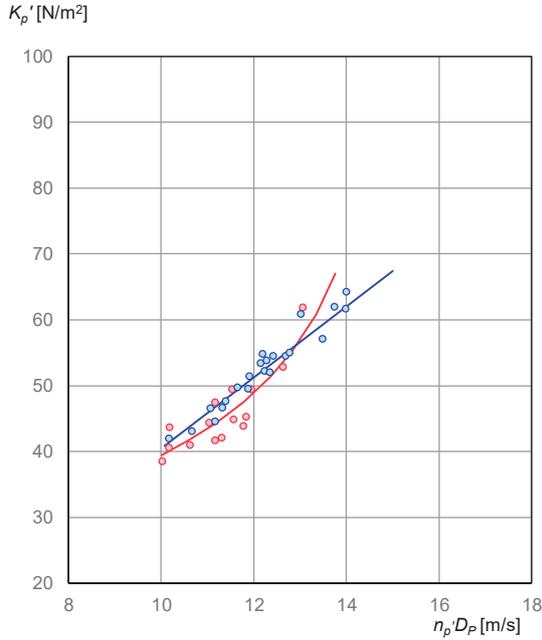


Fig. 9 Rearranged chart of estimating  $a_E$  (Blue; reference 10), Red; reference 11).

Fig. 10 Distribution of  $a_E$ . (Orange; full ships, Green; fine ships).

$$a_E = \frac{1}{K_p} \frac{MCR}{V_{des} D_p^2} \tag{34}$$

$$K_p = K_{p1}(n_p D_P) + K_{p0} \tag{35}$$

Table 3 Coefficients for  $a_E$ .

	$K_{p1}$ [Ns/m <sup>3</sup> ]	$K_{p0}$ [N/m <sup>2</sup> ]
Full ships	8.0	-31.0
Fine ships	7.0	-33.0

To make validation of the formula, estimation error ( $Err$ ) for  $a_E$  is evaluated at first. Difference between  $a_{Eest}$ , which is estimated from Eq. (34), and the actual  $a_E$  is determined using Eq. (36).

$$Err = \frac{a_{Eest} - a_E}{a_E} \tag{36}$$

From the comparison, it was found that  $Err$  ranged from -2 to 9% (average 4%) for full ships and from -1 to 5% (average 2%) for fine ships.

Next, the effect of  $a_E$  on propeller efficiency in open water ( $\eta_0$ ) is evaluated. The propeller was a four-blade propeller for a bulk carrier with a pitch ratio of 0.844 and  $a_E$  of 0.425. The propeller characteristics in open water are shown in Fig. 11. Estimated  $a_E$  was obtained using UNITAS, where  $a_E$  was derived from Eq. (34) ( $a_{Eest}$ ), and POT was obtained from tank tests. The difference in  $\eta_0$  was about 0.72% at the propeller advance ratio  $J = 0.6$ , while  $a_{Eest}$  was 0.464 (9% larger than the true value). Therefore, Eq. (34) is suitable to estimate the propeller characteristics in open water.

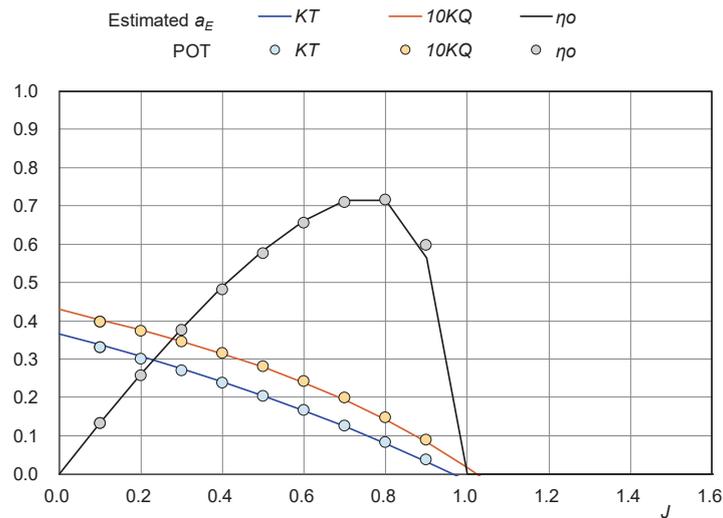


Fig. 11 Effect of  $a_E$  on propeller characteristics in open water.

### 2.9 Rudder area

#### 1) Estimation at design load condition

Rudder dimensions are required for estimating rudder forces. If the dimensions are not known, they should be estimated. The rudder dimensions to be estimated are illustrated in Fig. 12.

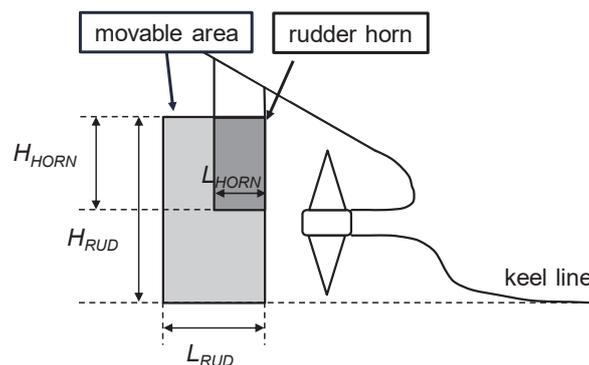


Fig. 12 Rudder dimensions at design load condition.

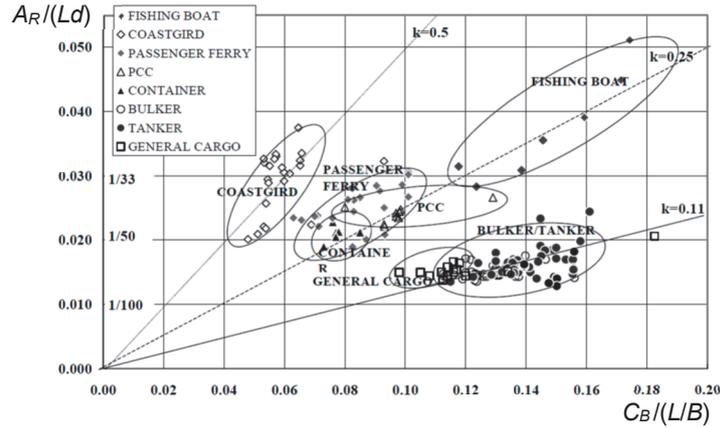


Fig. 13 Rudder movable area<sup>12)</sup>.

From the chart<sup>12)</sup> shown in Fig. 13, the rudder movable area ( $A_R$ ) can be estimated by  $d_m$ ,  $C_B$ , and  $B_{max}$ . The  $A_R$  can be obtained from Eq. (37) by using the correction factor ( $R_k$ ) for each ship type. The  $R_k$  is expressed using Eq. (38)

$$A_R = R_k C_B B_{max} d_m \tag{37}$$

$$R_k = \begin{cases} 0.11 & \text{Bulker and Tanker} \\ 0.25 & \text{Container ship and RoRo ship} \end{cases} \tag{38}$$

The total rudder area ( $A_{RT}$ ) including the rudder horn can be estimated using Eq. (39) using the correction factor for the total rudder area ( $R_{kt}$ ). The  $R_{kt}$  is derived from the recent ship data and expressed using Eq. (40).

$$A_{RT} = R_{kt} A_R \tag{39}$$

$$R_{kt} = \begin{cases} 1.20 & \text{Bulker, Tanker and Container ship} \\ 1.15 & \text{RoRo ship} \end{cases} \tag{40}$$

The rudder height ( $H_{RUD}$ ) can be estimated using Eq. (41) where  $k_{dr}$  is the empirical coefficient derived from the recent ship data and expressed using Eq. (42). The aspect ratio of the rudder ( $\Lambda_R$ ) is calculated using Eq. (43) and the height of the rudder horn ( $H_{HORN}$ ) can be set to half  $H_{RUD}$  by using Eq. (44).

$$H_{RUD} = k_{dr} d_m \tag{41}$$

$$k_{dr} = \begin{cases} 0.75 & \text{Bulker and Tanker} \\ 0.85 & \text{Container ship} \\ 0.90 & \text{RoRo ship} \end{cases} \tag{42}$$

$$\Lambda_R = \frac{H_{RUD}^2}{A_{RT}} \tag{43}$$

$$H_{HORN} = 0.5 H_{RUD} \tag{44}$$

The cord length of the rudder ( $L_{RUD}$ ) and length of the rudder horn ( $L_{HORN}$ ) can be estimated using Eqs. (45) and (46), respectively.

$$L_{RUD} = \frac{A_{RT}}{H_{RUD}} \quad (45)$$

$$L_{HORN} = \frac{(R_{kl} - 1)A_R}{H_{HORN}} \quad (46)$$

## 2) Estimation at voyage load condition

During the voyage, the effective rudder area differs from the rudder area due to the draught and trim change. When  $d_a$  is larger than  $H_{RUD}$ , the rudder area is used at the design load condition. However, when  $d_a$  is smaller than  $H_{RUD}$ , the rudder area should be estimated. The rudder dimensions at voyage load condition are shown in Fig. 14.

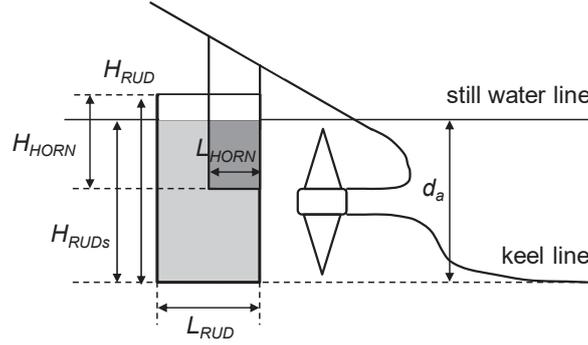


Fig. 14 Rudder dimensions at voyage load condition.

Assuming the  $H_{RUD}$  during the voyage ( $H_{RUDs}$ ) is equal to  $d_a$ , the rudder movable area ( $A_{Rs}$ ), total rudder area ( $A_{RTs}$ ) and aspect ratio of the rudder ( $\Lambda_{Rs}$ ) during the voyage are estimated from the geometric relations expressed using Eqs. (48), (49), and (50), respectively.

$$H_{RUDs} = d_a \quad (47)$$

$$A_{Rs} = 0.5H_{RUD}L_{RUD} + (d_a - 0.5H_{RUD})(L_{RUD} - L_{HORN}) \quad (48)$$

$$A_{RTs} = H_{RUDs}L_{RUD} \quad (49)$$

$$\Lambda_{Rs} = \frac{H_{RUDs}^2}{A_{RTs}} \quad (50)$$

## 2.10 Specific fuel consumption

To estimate fuel consumption, it is necessary to input the specific fuel consumption ( $SFC$ ). This value depends on the power and revolution rate of the engines. Normally, it is evaluated by the change in the engine output since information of the two parameters cannot be obtained. The change in  $SFC$  with respect to the engine output shifts depending on the fuel used, so it is better to estimate from the operation data. However, if this is not available, estimation is necessary.

The relationship between the output of the main engines ( $BHP$ ) and  $SFC$  can be expressed using a quadratic expression (Eq. (51)) with the minimum  $SFC$  at 75%MCR. The relationship is shown in Fig. 15.

$$SFC = a(BHP - 0.75MCR)^2 + b \quad (51)$$

where  $a$  and  $b$  are the coefficients determined in Table 4. If the actual  $SFC$  at 75%MCR is known, it should be used as  $b$  in Eq. (51).

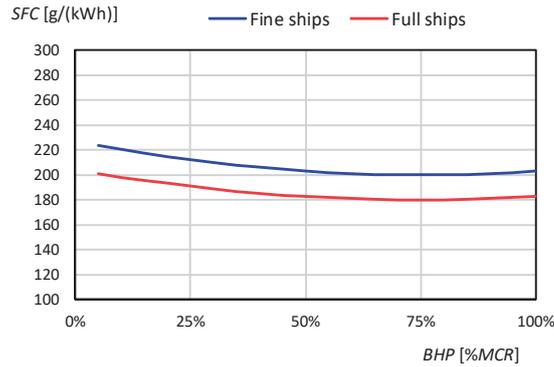


Fig. 15 Estimation of *SFC*.

1) Full ships; tanker and bulker

$b=170.0$  g/(kWh) and *SFC* at 50%MCR and MCR set 1.5% larger than *SFC* at 75%MCR.

2) Fine ships; container and RoRo ships

$b=200.0$  g/(kWh) and *SFC* at 50%MCR and MCR set 1.5% larger than *SFC* at 75%MCR.

Table 4 Coefficients for estimating *SFC*.

Ship type	$a$ [g/(kW <sup>3</sup> h)]	$b$ [g/(kWh)]
Full ships	$0.24b/MCR^2$	170.0
Fine ships	$0.24b/MCR^2$	200.0

### 3. Comprehensive evaluation

Using these empirical formulae, a comprehensive evaluation was carried out<sup>13)</sup> for the purpose of developing an advanced weather routing system. The evaluation was carried out using a 200-m-long RoRo vehicle carrier. The dimensions and performance of the ship were estimated using the formulae shown in this paper since the weather routing service often cannot obtain the data. Five voyage simulations for ship speed, engine output, and fuel consumption were conducted and compared with the ship monitoring data obtained onboard. The estimated total fuel consumption for the five voyages varied from -2.6 to 1.7% of the measured value and its average was 0.5% of that.

It is found that the formulae shown in this paper are sufficient to simulate ship performance.

### 4. Conclusions

We developed empirical formulae for estimating ship performance that use recent ship data and geometric relationships.

Though improving the accuracy for estimating longitudinal centre of buoyancy is for future work, these empirical formulae are sufficiently accurate for estimating ship performance.

### Acknowledgements

The research was supported by JSPS KAKENHI Grant Numbers JP15H04218 and Program for Promoting Technological Development of Transportation (Ministry of Land, Infrastructure, Transport and Tourism of Japan).

## References

- 1) M. Tsujimoto, H. Orihara: [Performance prediction of full-scale ship and analysis by means of on-board monitoring \(Part 1 ship performance prediction in actual seas\)](#), Journal of Marine Science and Technology, open access (2018), 18p.
- 2) M. Tsujimoto, N. Sogihara, M. Kuroda, K. Kume and H. Ohba: A Practical Prediction Method for Self Propulsion Factors in Actual Seas, Proceedings of the Twenty-eighth (2018) International Ocean and Polar Engineering Conference, ISOPE-I-18-523 (2018), pp.863–870.
- 3) N. Sogihara and M. Tsujimoto: Development of VESTA and UNITAS v-Tools for evaluation of ship performance in actual seas (in Japanese), Proceedings of 12th Research Presenting Meeting of National Maritime Research Institute, PS-2 (2012), pp.3–7.
- 4) M. Tsujimoto, N. Sogihara, M. Kuroda and A. Sakurada: Ship Performance Simulator in Actual Seas -VESTA- (in Japanese), Papers of National Maritime Research Institute, Vo.15, No.4 (2016), pp. 55–65.
- 5) Y. Ichinose and K. Kume: A Program named "HOPE Light" for Optimizing Hull-Form Dimensions (in Japanese), Papers of National Maritime Research Institute, Vo.15, No.4 (2016), pp.13–25.
- 6) The Kansai Society of Naval Architects, Japan: Shipbuilding Design Handbook (in Japanese), 4th edition, Kaibundo publishing Co., Ltd. (1983).
- 7) T. Fujiwara, M. Ueno and Y. Ikeda: Cruising Performance of a Large Passenger Ship in Heavy Sea, Proceedings of the Sixteenth International Offshore and Polar Engineering Conference, ISOPE-I-06-187 (2006), pp. 304–311.
- 8) M. Ueno, F. Kitamura, N. Sogihara and T Fujiwara: A Simple Method to Estimate Wind Loads on Ships, Proceedings of the 2012 World Congress on Advances in Civil, Environmental, and Material Research (2012), pp. 2314–2322.
- 9) K. Ito: Simple Method of Computing Marine Propeller Dimensions (in Japanese), Journal of the Kansai Society of Naval Architects, Japan, Vol. 106 (1962), pp.1–6.
- 10) Shipbuilding text research group: Basics of merchant ship design (the first volume) (in Japanese), Seizando-Shoten Publishing Co., Ltd., (1979).
- 11) Shipbuilding text research group: Basics knowledge of merchant ship design (in Japanese), Seizando-Shoten Publishing Co., Ltd., (2001).
- 12) Y. Yoshimura: Principle of rudder and its design (in Japanese), Bulletin RAN, No.55 (2002), pp. 3–11.
- 13) M. Tsujimoto, T. Matsuzawa, N. Sogihara, K. Hirayama, Y. Sugimoto, K Hasegawa and K. Yokokawa: Advanced Weather Routing System for Ships in Actual Seas - Development and Validation by a Ship, Proceedings of the 16th World Congress of the International Association of Institutes of Navigation 2018 (2018), p.10.